

SAMOSA retracker for SAR Altimeter observations over water

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- Introduction
- SAMOSA Overview
- Problem Formulation
- Theoretical Model for the Mean Return Echo Over Water Surfaces
- Conclusions

- **SAMOSA (ESA):** "Development of SAR Altimetry Studies and Applications over Ocean, Coastal zones and Inland waters"

- This presentation concentrates on → progress towards the development of a **theoretical model for the mean return waveform from a SAR altimeter over water surfaces**



- **Development of a re-tracking methodology (based on MLE)**



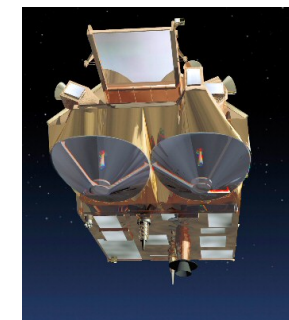
Theoretically tested
Cramer-RAO Bound

Experimentally tested



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- The application of SAR techniques to classical radar altimetry offers a potential solution to significantly enhance Earth surface mapping
- CryoSat (2009) will be the first satellite to provide such data
- This data is of great interest to the Hydrosphere and Oceanographic communities, since it would allow quantitative assessment of expected enhanced altimetric capabilities in **coastal monitoring**, ocean floor topography, gravity field and inland water monitoring.
- **SAMOSA FOCUS:** analyze the potentialities of advanced SAR Altimetry over water surfaces.



© Cryosat - ESA

CryoSat was designed for Cryosphere applications



Requirements for the application of SAR mode observations for **oceanography:**



1. Retracker adapted to the specific nature of SAR altimeter echoes
2. Theoretical Model for the Mean Return Echo Over Water Surfaces in the same spirit set by conventional altimeters [Brown, 1977] [Hayne, 1980]

- **SAR Altimeter** (a.k.a Delay/Doppler altimeter) introduced by Dr. Keith Raney (1998)

- Key innovation is the introduction of along track processing:

- Increased Resolution
- Multi-look processing

- Technique requires echo delay compensation analogous to Range Cell Migration correction (conventional SAR)

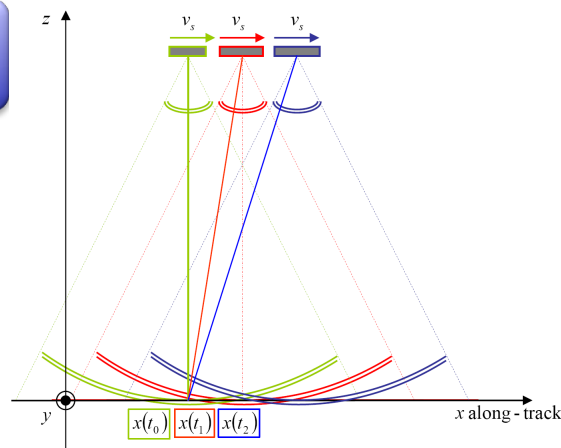
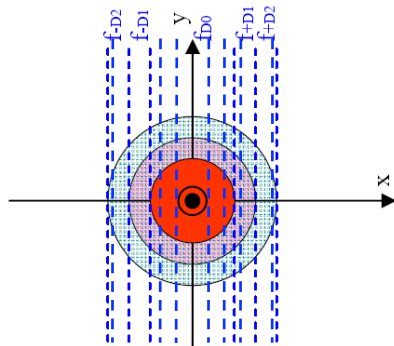
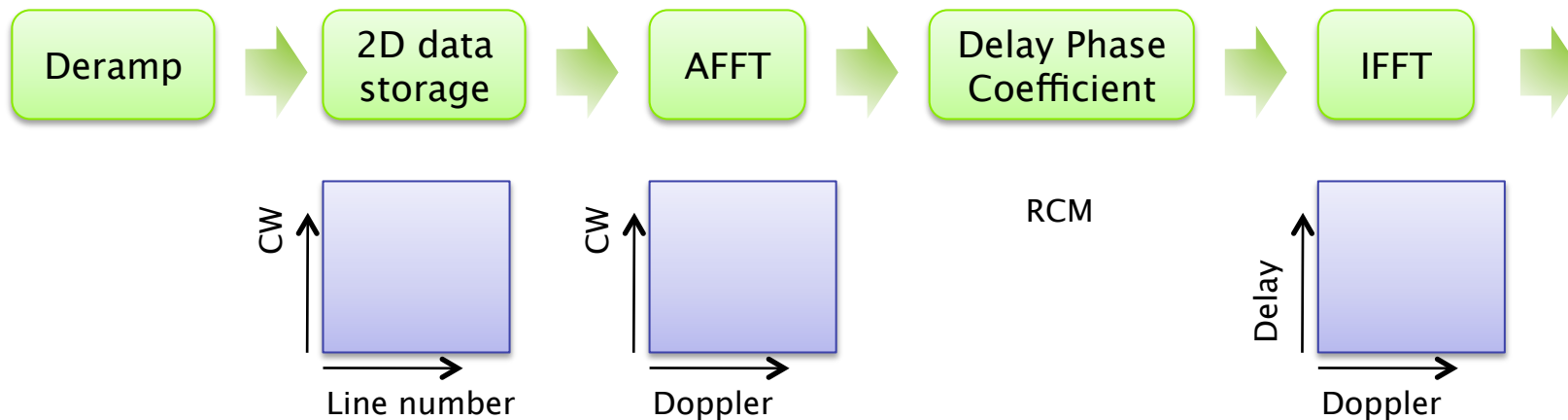


- Spatial resolution is increased in the along-track dimension.
- Accumulation of more statistically independent looks for each scattering area



- Better speckle reduction → finer precision of altimetric measurements.

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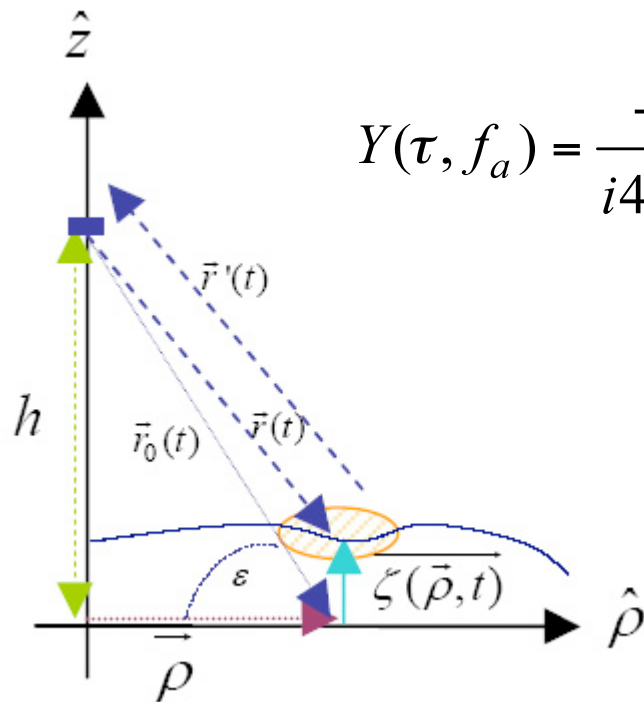


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After the accumulation block the received intensity shall be written as:

$$I_R = Y(\tau, f_a)Y^*(\tau, f_a)$$

$$Y(\tau, f_a) = \frac{-\Re\lambda_0}{i4\pi\sqrt{4\pi}} \int_{Area} \frac{1}{r^2} G(\vec{\rho}) \chi(\tau, f_a) \frac{q^2}{q_z} d^2\rho$$



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If Brown approach is applied



Calculate the mean of the incoherent addition of an infinite number of echoes

$$E[I_R]_{\zeta(\vec{\rho}, t)} = E[Y(\tau, f_a) Y^*(\tau, f_a)]_{\zeta(\vec{\rho}, t)}$$



$$E[I_R] = P_{FS}(\tau, f_a) ** S_R(\tau, f_a) * \left(\frac{c}{2}\right) P_z\left(\frac{c\tau}{2}\right)$$

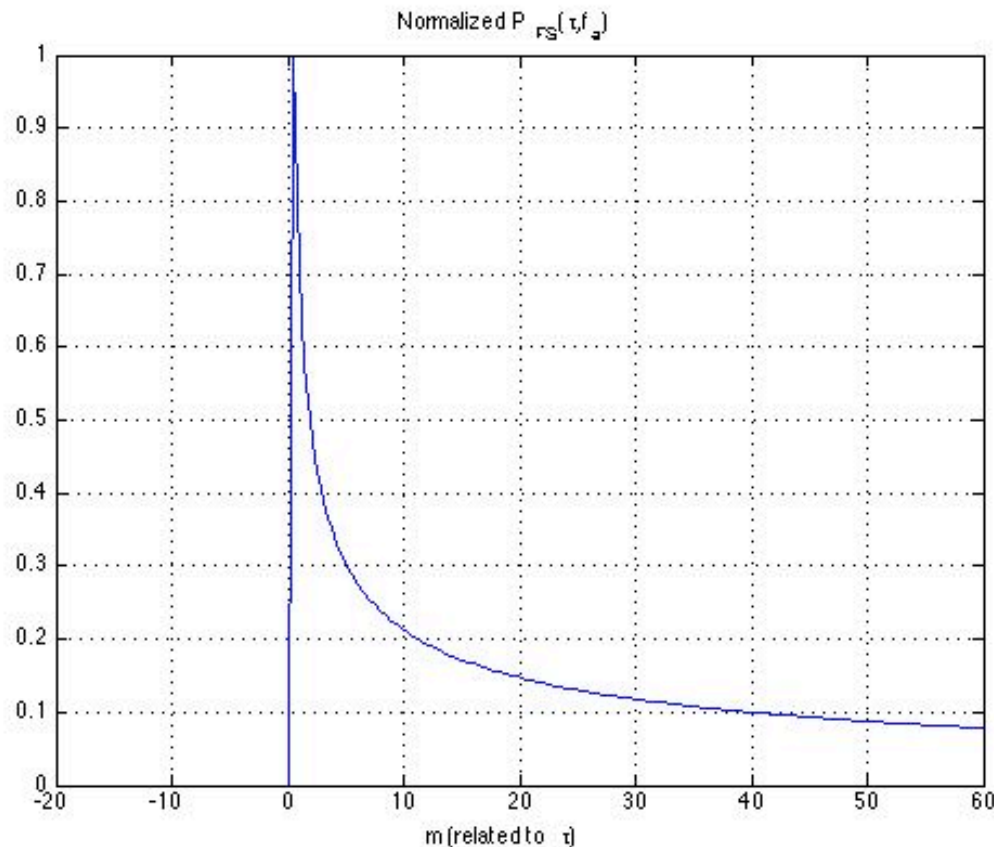
Flat Surface
Impulse Response

System point target
response

Surface elevation
p.d.f

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$$P_{FS}(\tau, f_a) = \frac{\lambda_0^2}{(4\pi)^2} \int G^2(\vec{\rho}) \frac{1}{r^4} \sigma_0(\vec{\rho}) \delta^2(s\tau - \tau_s(\vec{\rho}), f_a - f_s(\vec{\rho})) d^2\rho$$

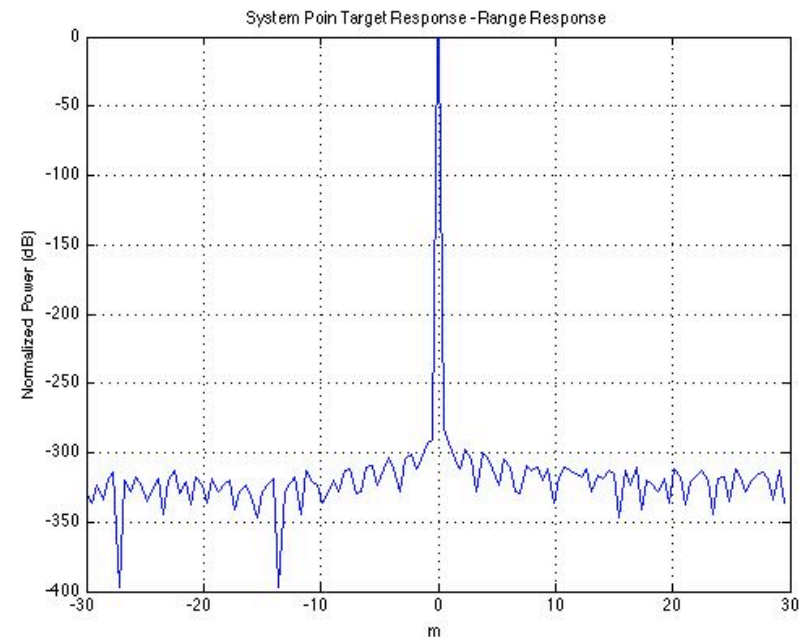
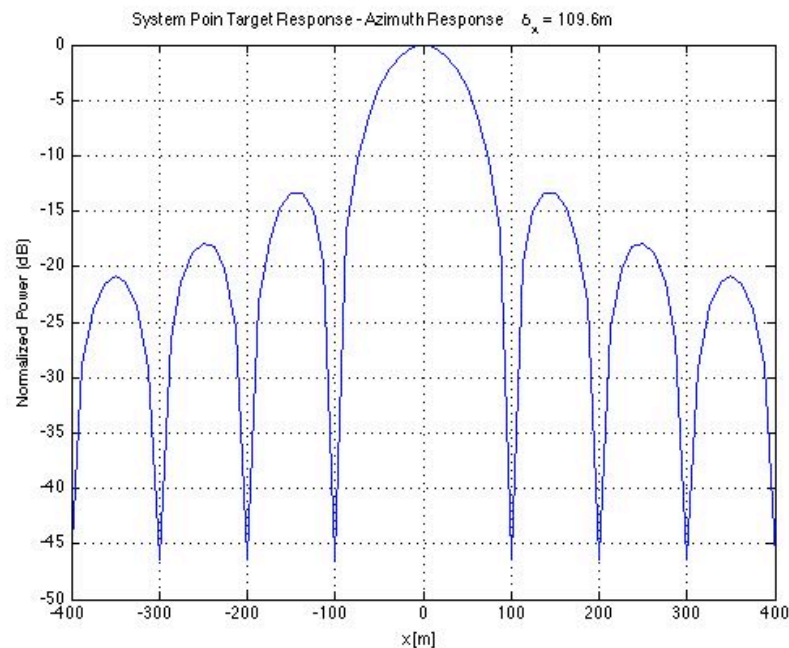


$$\tau_s = \frac{s}{hc} (y^2 + (h - z)^2 - h^2)$$

$$f_s = \alpha f_D$$

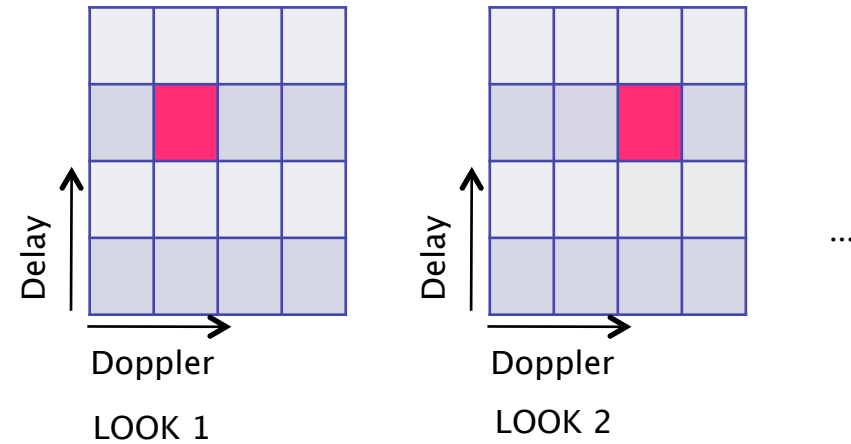
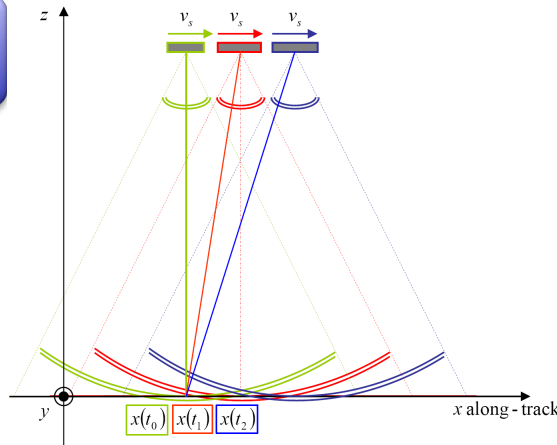
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$$S_R(\tau, f_a) = T^2 \tau_u^2 \text{sinc}^2(T f_a) \text{sinc}^2(\tau_u s \tau)$$



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Multi-Look



$$I_{ML} = \sum_{m=-M/2}^{M/2-1} Y(\tau, f_a - m\Delta f) Y^*(\tau, f_a - m\Delta f)$$

$$E[I_{ML}]_{\zeta(\vec{\rho}, t)=z} = \sum_{m=-M/2}^{M/2-1} E[Y(\tau, f_a - m\Delta f) Y^*(\tau, f_a - m\Delta f)]_{\zeta(\vec{\rho}, t)}$$

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- The SAR Altimeter waveform satisfies Hayne's model with different: Flat surface impulse response and System point target Response adapted to the SAR geometry
- The Flat surface impulse response is along track and across track dependent
- The System point target response of the SAR altimeter results in finer resolution which will be of great interest to the scientific coastal altimetry community

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